

Assume that at the concentrations we are using, the following is the only equilibrium that matters.

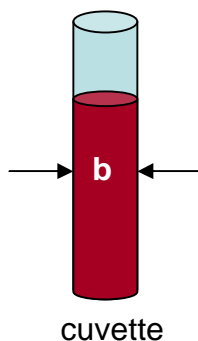
	$\text{Fe}^{3+}(\text{aq})$	$+$	$\text{SCN}^{-}(\text{aq})$	$\rightleftharpoons$	$\text{Fe-SCN}^{2+}(\text{aq})$	
Initial	$[\text{Fe}^*]$		$[\text{SCN}^*]$		0	Initially there is no Fe-SCN complex, but it forms in order to establish this equilibrium. To do this, some of the original $\text{Fe}^{3+}$ and $\text{SCN}^{-}$ (x each) must be consumed.
Change	-x		-x		x	
Equilibrium	$[\text{Fe}^*] - x$		$[\text{SCN}^*] - x$		x	

$$K_C = \frac{[\text{FeSCN}^{2+}]_{\text{eq}}}{[\text{Fe}^{3+}]_{\text{eq}} [\text{SCN}^{-}]_{\text{eq}}}$$

$A_{447}$  is the absorbance of  $\text{FeSCN}^{2+}$  at this wavelength. This is directly related to concentration according to the equation

$$A = \epsilon b [\text{FeSCN}^{2+}]$$

Bright red  $\text{FeSCN}^{2+}$  absorbs light at 447 nm.



**b** is the path length that the light beam travels through. This is a constant and in this case is 1 cm.

$\epsilon$  is the molar absorptivity of the  $\text{FeSCN}^{2+}$  complex at 447 nm. It too is a constant at this wavelength for this system.

Rearranging this equation gives

$$[\text{FeSCN}^{2+}]_{\text{eq}} = x = \frac{A_{447}}{\epsilon b}$$

$$[\text{Fe}^{3+}]_{\text{eq}} = [\text{Fe}^*] - x$$

$$[\text{SCN}^{-}]_{\text{eq}} = [\text{SCN}^*] - x$$

Plugging these into our  $K_C$  expression gives

$$K_C = \frac{x}{([\text{Fe}^*] - x) ([\text{SCN}^*] - x)} = \frac{x}{[\text{Fe}^*][\text{SCN}^*] - [\text{Fe}^*]x - [\text{SCN}^*]x + x^2}$$

Experience has shown that  $\epsilon$  for  $\text{FeSCN}^{2+}$  is an enormous number, about 10,000 times larger than  $A_{447}$ . Given this idea

$$x = \frac{A_{447}}{\epsilon b} = \text{very small (not zero, but very small)}$$

This means that  $x^2 \sim 0$  or small enough to neglect in the expanded  $K_C$  expression above.

$$K_C = \frac{x}{[\text{Fe}^*][\text{SCN}^*] - [\text{Fe}^*]x - [\text{SCN}^*]x + x^2} \sim \frac{x}{[\text{Fe}^*][\text{SCN}^*] - [\text{Fe}^*]x - [\text{SCN}^*]x}$$

Collect terms in the denominator on the right

$$K = \frac{x}{[\text{Fe}^*][\text{SCN}^*] - ([\text{Fe}^*] + [\text{SCN}^*])x}$$

Cross multiply

$$K \left( [\text{Fe}^*][\text{SCN}^*] - ([\text{Fe}^*] + [\text{SCN}^*])x \right) = x = K[\text{Fe}^*][\text{SCN}^*] - Kx([\text{Fe}^*] + [\text{SCN}^*])$$

The real expression for x needs to be substituted at this point ( $x = A/\epsilon b$ )

$$x = \frac{A}{\epsilon b} = K[\text{Fe}^*][\text{SCN}^*] - K \frac{A}{\epsilon b} ([\text{Fe}^*] + [\text{SCN}^*])$$

Multiply through by  $\epsilon b$

$$A = K\epsilon b [\text{Fe}^*][\text{SCN}^*] - K A ([\text{Fe}^*] + [\text{SCN}^*])$$

Divide through by  $[\text{Fe}^*][\text{SCN}^*]$ , reorder terms on the right.

$$\frac{A}{[\text{Fe}^*][\text{SCN}^*]} = -K \frac{A ([\text{Fe}^*] + [\text{SCN}^*])}{[\text{Fe}^*][\text{SCN}^*]} + K\epsilon b$$

This is now a linear equation if you look carefully.

$$\frac{A}{[\text{Fe}^*][\text{SCN}^*]} = -K \frac{A ([\text{Fe}^*] + [\text{SCN}^*])}{[\text{Fe}^*][\text{SCN}^*]} + K\epsilon b$$

**y**
**=**
**m**
**x**
**+**
**b**

